

# Force, Switched and Mixed Hybrid Simulation Control in OpenFresco

Dr. Hong Kim, Systems Engineer  
Osisoft, San Ramon, CA, USA

Dr. Bozidar Stojadinovic, Professor  
IBK, ETH Zürich, Switzerland

# Hybrid Simulation

- ◆ A dynamic testing method:
  - Complements the shaking table and quasi-static testing methods
- ◆ Specimen is a hybrid model of the prototype:
  - Integrates numerical and physical sub-models
- ◆ Developed since mid-1970's
  - Almost in parallel with shaking tables!

# Dynamic Test Methods

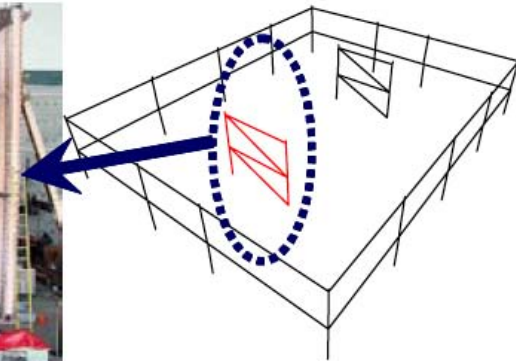
## Shaking Table

◆ E-Defense



## Hybrid Simulation

◆ NCREE PISA system

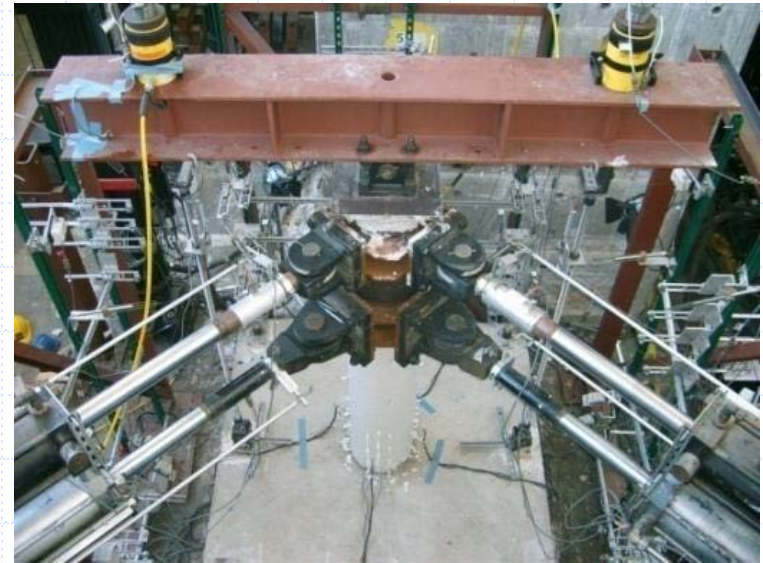


# Control in Hybrid Simulation

- ◆ Defines how the physical and the numerical sub-structures are integrated:
  - Displacement: enforcing compatibility
  - Forces: enforcing equilibrium
- ◆ Defines how the servo-hydraulic system is driven:
  - Displacement/position feedback
  - Force feedback

# Displacement Control

- ◆ Conventional hybrid simulation is conducted in displacement control
- ◆ Advantages:
  - Servo-hydraulic system feedback
  - Numerical model implementation



# Displacement Control

## ◆ Challenges:

- Stiff specimens
- Significant stiffness variations:
  - ◆ With direction of loading
  - ◆ Degradation due to damage
- Fast tests:
  - ◆ Dynamic effect in the physical sub-model
- Multiple DOFs



# Force Control

- ◆ Control system imposes force on the physical sub-model
- ◆ Challenges:
  - Acquiring the force targets:
    - ◆ Most numerical models are implemented in “displacement” control
  - Closing the feedback loop:
    - ◆ Stiffness of the specimen and loading system impacts the control loop gain
    - ◆ Low gain needed for stability: poor tracking
    - ◆ Friction and stick/slip behavior affect performance
    - ◆ Oscillations in feedback signal from load cells

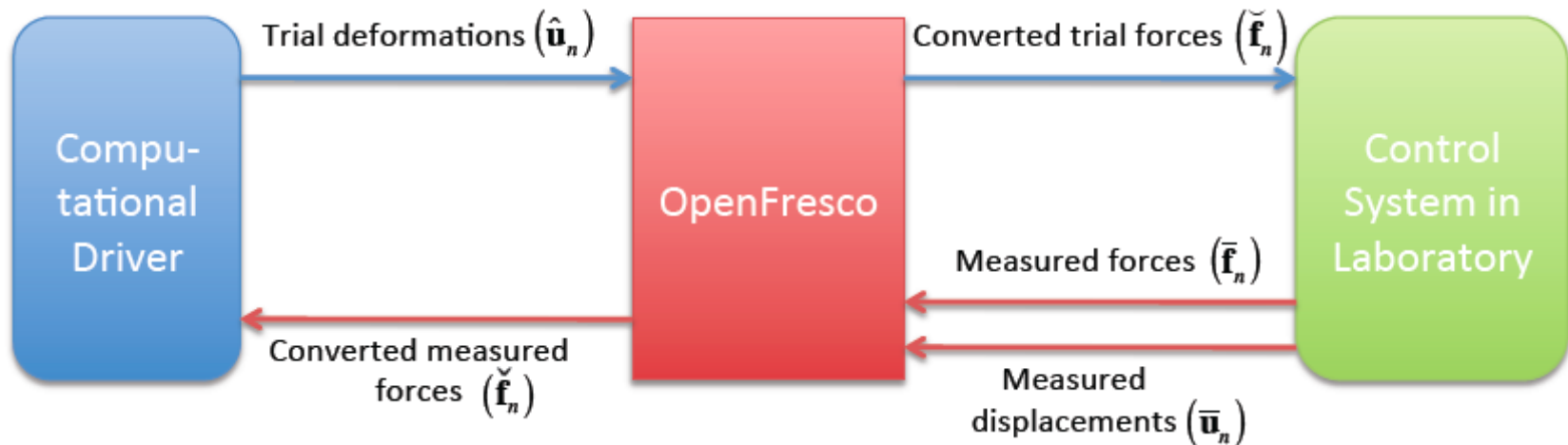
# Force Control: Implementation

- ◆ Compatibility (of displ.) methods:
  - Tangent-based:
    - ◆ Broyden, BFGS, Intrinsic, Transpose
  - Krylov sub-space
  - Compatible with numerical model implementation methods
- ◆ Equilibrium (of forces) methods:
  - Derived from flexibility FEM formulation
  - Require compatible numerical models



# Force Control: OpenFresco

## ◆ Compatibility methods



## ◆ Conversions implemented in the *ExperimentalSignalFilter* class

# Force Control: OpenFresco

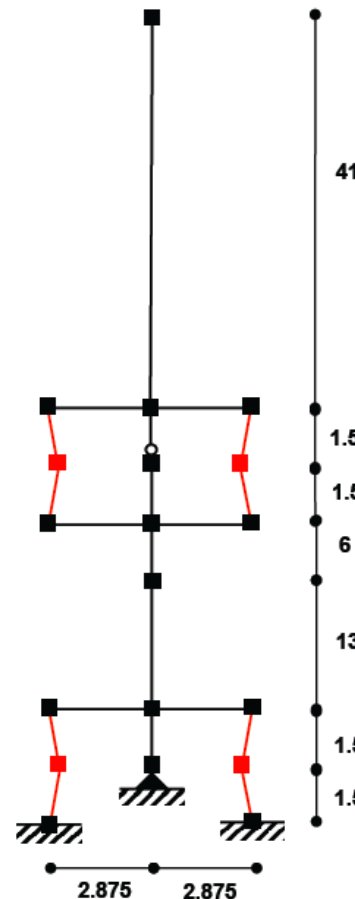
## ◆ Equilibrium methods

## ◆ Implemented in:

- Flexibility (force) based FEA package in Matlab (based on OpenSees structure)
- OpenFresco force-based predictor and corrector in Simulink/Stateflow
- OpenFresco force experimental control sub-class

# Force Control: Validation and Verification

## ◆ 2-DOF specimen



$$T_1 = 0.55\text{sec}$$

$$T_2 = 0.20\text{sec}$$

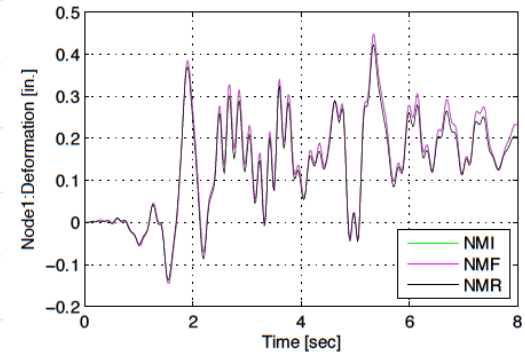
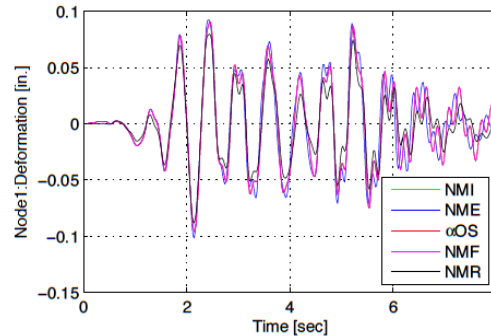
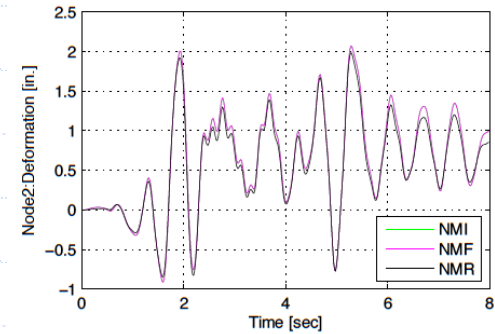
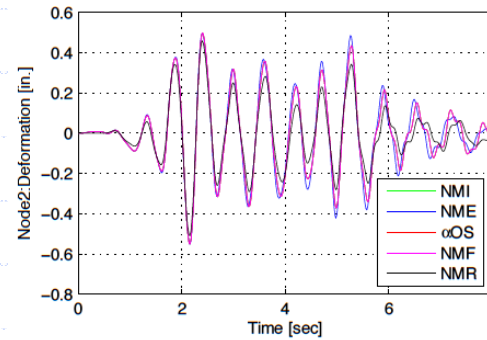
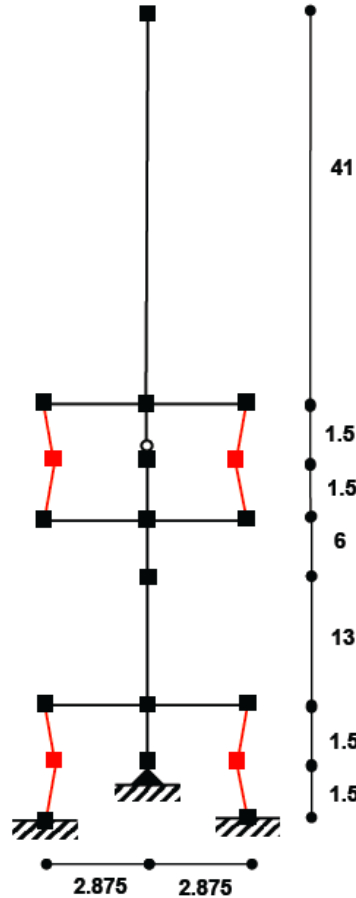
$$m = \begin{bmatrix} 0.01 & 0 \\ 0 & 0.1 \end{bmatrix}$$

Soft

$$k = \begin{bmatrix} 3.4 & -12 \\ -12 & 84 \end{bmatrix}$$

Stiff

# Force Control: Validation and Verification



Linear response

Non-linear response

# Force Control: Validation and Verification

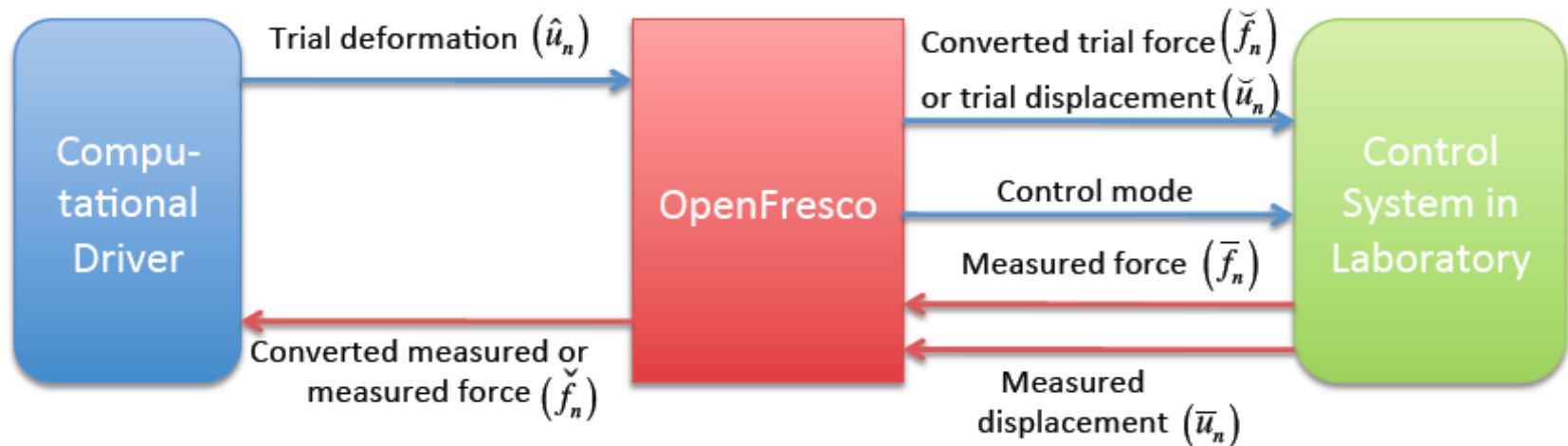
## ◆ Node 1 displacement errors

| Control method     | NME (in.)             | $\alpha$ OS (in.)     | NMF (in.)             | NMR (in.)             |
|--------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| DC-Min             | $2.97 \times 10^{-7}$ | $1.32 \times 10^{-8}$ | $3.90 \times 10^{-6}$ | $2.45 \times 10^{-5}$ |
| DC-Mean            | 0.163                 | 0.147                 | 0.0307                | 0.379                 |
| DC-Max             | 0.419                 | 0.337                 | 0.153                 | 0.664                 |
| CFC:BFGS-Min       | $3.75 \times 10^{-8}$ | 1.15e-08              | $4.19 \times 10^{-5}$ | $1.81 \times 10^{-5}$ |
| CFC:BFGS-Mean      | 0.0594                | 0.0319                | 0.0519                | 0.110                 |
| CFC:BFGS-Max       | 0.251                 | 0.166                 | 0.182                 | 0.241                 |
| CFC:Intrinsic-Min  | N/A                   | 2.92e-08              | N/A                   | $8.23 \times 10^{-6}$ |
| CFC:Intrinsic-Mean | N/A                   | 0.0527                | N/A                   | 0.0750                |
| CFC:Intrinsic-Max  | N/A                   | 0.229                 | N/A                   | 0.191                 |

# Switch Control

- ◆ Control mode of an actuator changes during hybrid simulation
  - Different specimen stiffness, depending on loading direction
- ◆ Challenges:
  - Switch trigger algorithm:
    - ◆ Trial force (Point Switching Strategy)
    - ◆ Secant stiffness (Secant Switching Strategy)
  - Stable and fast switch
  - Accurate force and displacement control

# Switch Control: Implementation



## ◆ Compatibility methods:

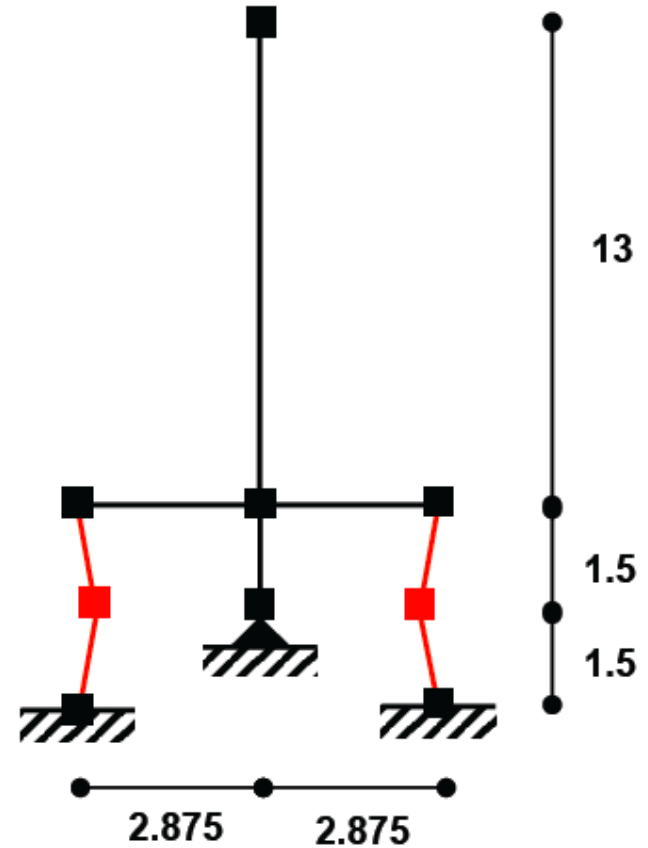
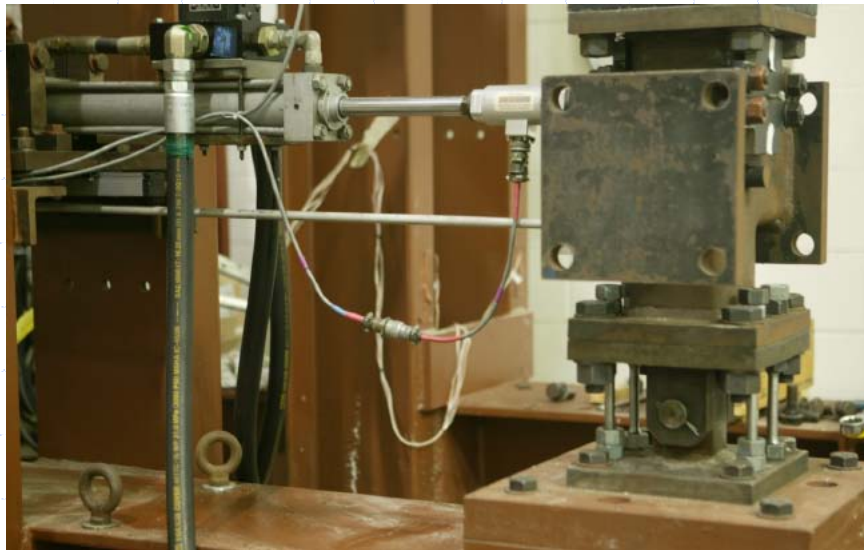
- Extended

## ◆ Equilibrium methods:

- Extended

# Switch Control: Validation and Verification

## ◆ 1-DOF specimen





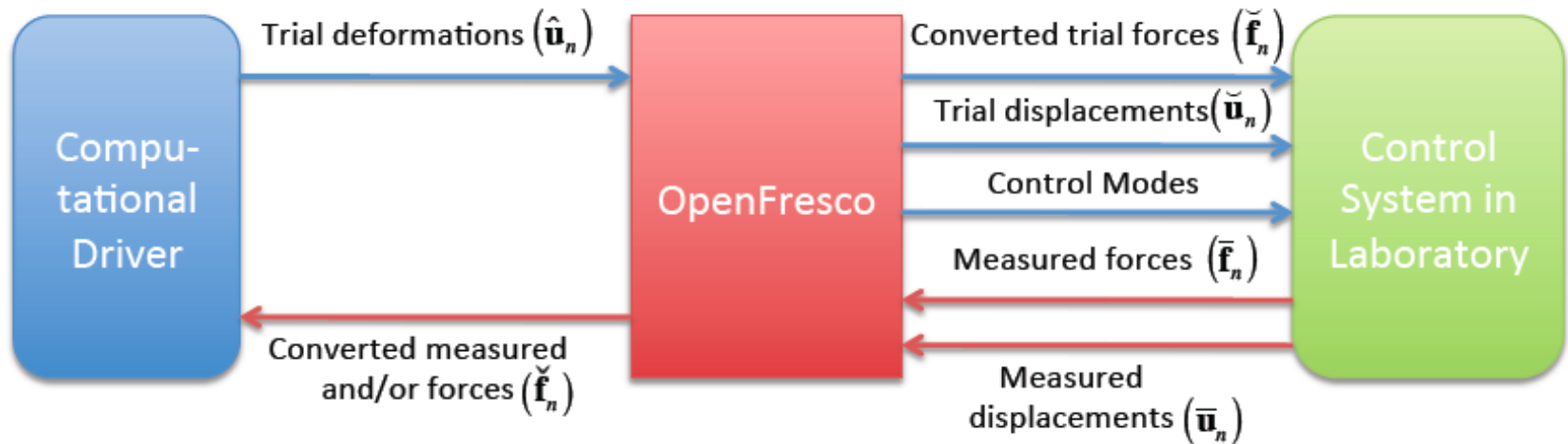
# Switch Control: Validation and Verification

| Control method | NME (in.)             | $\alpha$ OS (in.)     | NMF (in.)             | NMR (in.)             |
|----------------|-----------------------|-----------------------|-----------------------|-----------------------|
| DC-Min         | $2.84 \times 10^{-5}$ | $7.30 \times 10^{-7}$ | $1.64 \times 10^{-5}$ | $1.68 \times 10^{-5}$ |
| DC-Mean        | 0.0266                | 0.0288                | 0.114                 | 0.0711                |
| DC-Max         | 0.116                 | 0.118                 | 0.357                 | 0.253                 |
| CFC-Min        | N/A                   | N/A                   | $1.14 \times 10^{-5}$ | N/A                   |
| CFC-Mean       | N/A                   | N/A                   | 0.0409                | N/A                   |
| CFC-Max        | N/A                   | N/A                   | 0.143                 | N/A                   |
| PSC-Min        | $2.12 \times 10^{-5}$ | $6.34 \times 10^{-6}$ | $2.11 \times 10^{-5}$ | $2.49 \times 10^{-5}$ |
| PSC-Mean       | 0.0410                | 0.0816                | 0.0433                | 0.0422                |
| PSC-Max        | 0.104                 | 0.300                 | 0.204                 | 0.147                 |
| SSC-Min        | $8.00 \times 10^{-6}$ | $1.40 \times 10^{-5}$ | $6.67 \times 10^{-5}$ | $6.94 \times 10^{-6}$ |
| SSC-Mean       | 0.0341                | 0.0315                | 0.0397                | 0.0419                |
| SSC-Max        | 0.112                 | 0.122                 | 0.177                 | 0.150                 |
| EFC-Min        | N/A                   | N/A                   | N/A                   | $1.28 \times 10^{-4}$ |
| EFC-Mean       | N/A                   | N/A                   | N/A                   | 0.0922                |
| EFC-Max        | N/A                   | N/A                   | N/A                   | 0.280                 |
| EPSC-Min       | N/A                   | N/A                   | N/A                   | $6.02 \times 10^{-5}$ |
| EPSC-Mean      | N/A                   | N/A                   | N/A                   | 0.0339                |
| EPSC-Max       | N/A                   | N/A                   | N/A                   | 0.161                 |
| ESSC-Min       | N/A                   | N/A                   | N/A                   | $9.82 \times 10^{-6}$ |
| ESSC-Mean      | N/A                   | N/A                   | N/A                   | 0.0322                |
| ESSC-Max       | N/A                   | N/A                   | N/A                   | 0.0989                |

# Mixed Control

- ◆ Control modes on different degrees of freedom of the physical sub-model are different:
  - Each may be constant or switched
- ◆ Challenges:
  - All of the above, and...
  - Interaction of independent switching strategies
  - Time-step integration using measured or computed values?

# Mixed Control: Implementation

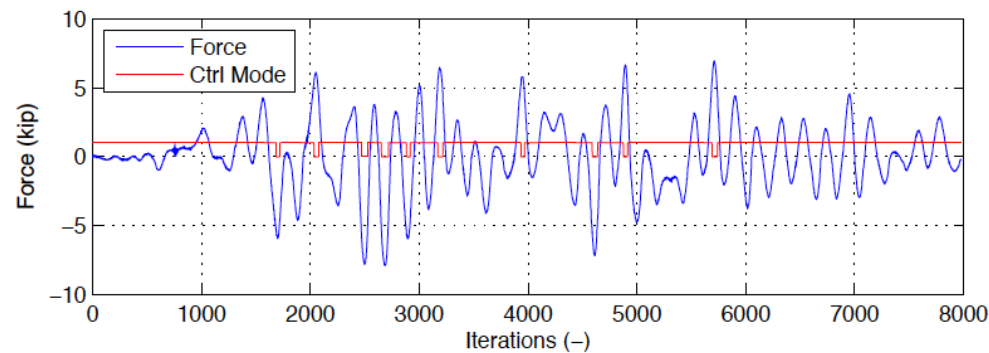


- ◆ Compatibility methods:
  - Extended further
- ◆ Equilibrium methods:
  - Extended further

# Mixed Control: Validation and Verification

## ◆ Node 1 displacement errors

| Control method           | NME                   | $\alpha$ OS           | NMF                    | NMR                    |
|--------------------------|-----------------------|-----------------------|------------------------|------------------------|
| PMC:Broyden-Min (in.)    | $1.41 \times 10^{-8}$ | $1.25 \times 10^{-9}$ | $8.67 \times 10^{-11}$ | N/A                    |
| PMC:Broyden-Mean (in.)   | $7.38 \times 10^{-4}$ | $9.33 \times 10^{-4}$ | $6.20 \times 10^{-4}$  | N/A                    |
| PMC:Broyden-Max (in.)    | 0.00587               | 0.0475                | 0.00570                | N/A                    |
| PMC:BFGS-Min (in.)       | $1.68 \times 10^{-9}$ | $4.84 \times 10^{-9}$ | $1.06 \times 10^{-8}$  | $1.98 \times 10^{-11}$ |
| PMC:BFGS-Mean (in.)      | $5.53 \times 10^{-4}$ | $5.67 \times 10^{-4}$ | $5.40 \times 10^{-4}$  | $5.57 \times 10^{-4}$  |
| PMC:BFGS-Max (in.)       | 0.00642               | 0.00497               | 0.00528                | 0.00684                |
| PMC:Intrinsic-Min (in.)  | $9.74 \times 10^{-9}$ | $5.14 \times 10^{-9}$ | $2.72 \times 10^{-9}$  | $3.32 \times 10^{-9}$  |
| PMC:Intrinsic-Mean (in.) | $7.47 \times 10^{-4}$ | $6.12 \times 10^{-4}$ | 0.00144                | $8.13 \times 10^{-4}$  |
| PMC:Intrinsic-Max (in.)  | 0.00579               | 0.00469               | 0.00565                | 0.00564                |



# Conclusions

- ◆ Force control implemented in OpenFresco:
  - Comparable to displacement control
  - Compatibility methods easier to implement
- ◆ Switch control implemented, too:
  - Stability and accuracy sensitive to integration method choice
- ◆ Mixed control implemented, but:
  - Difficulties with actuator interaction
- ◆ More work is needed...

# Conclusions

## ◆ This extension:

- Covers the duality between forces and displacements in structural mechanics
- Enables hybrid simulation of complex models under combined long- and short-term load effects

## ◆ Hybrid simulation advantage:

- Enables proof-testing of structural systems by physically testing only their crucial components, not entire systems

# Acknowledgements

- ◆ NEES
- ◆ PEER Center
  - Dr. Andreas Schellenberg
  - Dr. Tony Yang
- ◆ UC Berkeley
- ◆ ETH Zürich
- ◆ Kwang-Hua Foundation



# Thank you!

Development and operation of the *nees@berkeley* equipment site is sponsored by NSF.

<http://nees.berkeley.edu>

**NEES**

 **nees@berkeley**

The George F. Brown, Jr. Network for Earthquake